Real-Time Implementation of a General Model for Spatial Processing of Sounds

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Abstract
In 1982, one of the authors proposed a general model for spatial processing of sounds and included a partial implementation of it in the cmusic sound synthesis program[7]. This model is designed to simulate the most perceptible physical characteristics of a real or imaginary space relating to the localization of sound sources. The original model defines the acoustic space in two dimensions as an outer closed space (the illusory acoustic space) and an inner listening room (the intended performance space) with “openings” along its perimeter in the location of the speakers. The spatial impression is produced by simulating the direct radiation, early echoes, and global reverberation of a sound source as heard through each opening. This paper discusses our modifications of the original cmusic implementation: first, the algorithm runs in real-time, and second, we made additions that more satisfactorily realize the general model. Our implementations of the algorithm in Pd and Max/MSP are presented.

1 Introduction
This paper describes a real-time implementation of the “general model for spatial processing of sounds” proposed by one of the authors[7], who made a partial, though fairly complete, implementation of it as part of the cmusic package[6]. The general model draws on basic psychophysics of spatial perception (mostly the work of Gardner[4], Blauert[2], and Stevens[12]) and on work in room acoustics, particularly the work of Schroeder[10] and Moore[8] in developing realistic artificial reverberation.

The central concept of the algorithm is that of a “room within a room”. The inner room is the space delimited by the speakers which contains the listeners. The model simulates the behavior of the sound source within a user-defined virtual outer room, as heard from the inner room. The speakers act as “windows” through which sound from the outer room passes. The greatest strength of the algorithm, however, is that its spatial effects are minimally position dependent across an audience. This is achieved by focusing on simulating the physical characteristics of the real or imaginary space as heard in a defined performance space rather than from a vantage point of a single listener.

2 Moore’s Spatial Algorithm
Once the room dimensions are defined, the algorithm scales amplitude of the source signal to account for the directionality of the source. It then applies basic ray-tracing principles to simulate direct paths from the source to each speaker and early reflections of the source from each surface of the outer room to each speaker. (See Figure 1.)

2.1 Sound Source Model
In addition to x and y coordinates describing position of the source, the model uses three variables to simulate the radiation of the sound from a point source. The implementation of Moore’s spatial model in cmusic (called the “space unit generator”) receives a single audio input, and allows for an arbitrary numbers of radiation vectors (RV) as follows:

\[ \text{RV} = (x, y, \theta, \text{amp}, \text{back}), \]

(1)

where x and y are the location coordinates in meters with (0,0) at the center of the inner room, \( \theta \) is the source radiation direction, \text{amp} is the amplitude of the vector, and \text{back} is the relative radiation factor in the opposite direction of \( \theta \) (0 ≤ \text{back} ≤ 1). The following equation generates the amplitude scale factors which simulate a hypercardioid pattern:

\[ r(\phi) = \left[ 1 + \frac{(\text{back} - 1)(\theta - \phi)}{\pi} \right]^2 \]

(2)

where \( r(\phi) \) is the scalar for the simulated ray and \( \phi \) is the direction of the ray being simulated.
2.2 Direct and Reflected Path Calculations

Direct paths are calculated simply as straight lines from the source to each of the speakers and early reflections are calculated as two-part lines from the source reflected by the walls to each speaker. The differing impressions of the source at each speaker are accounted for by separate taps into a single delay line.

For direct paths, the distance from source to each speaker determines the delay time of that channel and influences the amplitude in accordance with the inverse power law connecting intensity with distance. Some psychoacoustic research suggests that an inverse cubic proportion may provide a more realistic impression[11].

The attenuation and delay times of the reflected rays are calculated according to the same algorithm used for direct paths. Early reflections provide one of the most important cues for source localization in space. The general model accounts for frequency-dependent attenuation of both direct and reflected rays due to absorption by air and the outer walls. In the cmusic implementation, frequency-dependent attenuation was omitted, since the loss of high frequencies made the spatial impression less distinct[5, p99]. For reasons of computational efficiency only first order reflections were implemented.

The model considers the outer walls of the inner room to be completely absorptive, which aids in clarity of spatial impression. This means that an essential condition for calculating both direct paths and early reflections is whether they “cut” the inner room. If the algorithm determines that a path “cuts” the inner room, that ray is discarded. Moore noted that a more sophisticated approach would be to model the diffraction of the path around the edge of the cutting surfaces but the additional computation may not be justified on perceptual grounds[7, p13].

Chowning points out that the pitch change due to Doppler effect is one of the most significant cues for sound movement in space[3]. Doppler pitch changes are a natural result of the delay set up in Moore's model.

2 New Modifications

In 1994, Ballan, Mossoni, and Rocchesso simplified Moore's spatial model for a moving sound source to run in real-time. Some of their simplifications include: (1) omitting direct ray calculation to the speaker located in the opposite quadrant of the source, (2) omitting rays reflected from any wall to the opposite speakers, and (3) calculating attenuation factors based on a simplified algorithm \( \text{amplitude} = 1 - \text{distortion} \). They observed: “These are strong simplifications, but the results still give a good spatial impression.”[1, p 476] We have achieved real-time performance without compromising the original model, and have added algorithms which implement the model more realistically.

3.1 Modifications for Real-Time Implementation

A computationally expensive aspect of Moore's spatial processing model is the calculation of delay times for direct and reflected sound rays. Once these values are calculated, there is no need to re-calculate them if the sound source does not move from its previous position. The computation of whether a direct or reflected sound ray intersects any one of these walls is another computationally expensive calculation. We have achieved real-time performance and more realistic results by modifying the original cmusic implementation in two ways. First, by down-sampling the path of sound sources and interpolating the delay times, and second, by improving inner room ray intersection detection algorithm. In this section we present and discuss the implementation of these two modifications.

3.1.1 Interpolation of Delay Times

In order to avoid discontinuities in the output signals, control signals to the space unit generator need to be continuous signals at audio rate. As mentioned above, the most computationally expensive part of Moore's algorithm is the calculation of delay times. In order to achieve real-time performance we down-sample the \( x \) and \( y \) signals to control rate (which means we are considering only the last coordinate in every block), and interpolate the resulting delay times and attenuation factors within each block.

3.1.2 Errors Introduced by the Interpolation Process

Error in the interpolation process introduces non-linear and non-realistic effects in the generated output; the most prevalent are in estimating the
position of the source and in introducing subtle timing asynchronies among the direct and reflected rays. When our block size is 64 samples, which is less than 1.5 milliseconds at SR=44, 100 Hz, a sound source is moving at 10 m/s, our error in localization will be less than 1.5 cm (1.5 ms * 10 m/s = 1.5 cm).

One way to interpret this error is that as the sound source moves faster, our interpolation algorithm changes a sound source from a point source to a small spherical source. No matter what type of interpolation we use, we will not be able to simulate the synchronization of all the direct and reflected rays.

Empirically we know that errors discussed in this section are very small and in most cases inaudible. The strength of Moore's spatial model is in localizing sound sources outside of the inner room where sound sources are considerably farther away from the listener, and therefore, more tolerant of localization and ray tracing errors.

### 3.2 Improved Ray Intersection Algorithm

The original spatial model defines an inner room which does not allow sound to travel through its walls. The cmusic implementation did not account for any diffraction of sound and used a fixed 50 millisecond crossfade time for turning sound rays on and off, but he noted that using a diffraction model may yield better results.

Diffraction of sound is a complex frequency dependent phenomenon. However, we implemented a simple diffraction model which produces attenuation values based on where a sound ray intersects a wall. Thus, the crossfade periods become related to the speed of the sound source. We used the distance from where a sound ray intersects a wall to the corner of the wall as a measure to calculate the diffraction attenuation factor according to the following equation:

\[
da = \begin{cases} 
0 & \text{when } TH < ds, \\
\left(\frac{TH - ds}{TH}\right)^{CF} & \text{when } 0 < ds < TH.
\end{cases}
\]  

where \(da\) is the diffraction attenuation factor, \(ds\) is the distance from where the sound ray intersects a wall to the corner of the wall, \(TH\) is the diffraction threshold variable, and \(CF\) is the crossfade exponential factor.

In listening to the results, we found the spatialization effects to sound more realistic than the results obtained by the original cmusic ray intersection detection implementation. We also found the two variables \(TH\) (diffraction threshold) and \(CF\) (crossfade exponential factor), in conjunction with the Direct variable, useful for fine tuning the spatialization effects in different performance spaces\(^1\). We have also improved the performance of the ray intersection algorithm by rewriting it with more simple arithmetic operations compared to the cmusic version.

### 3.3 Additional Improvements

We have also improved the quality of the interpolation of audio delay line for simulating the direct and reflected sound rays. The original cmusic implementation used linear interpolation. At fairly high speeds of the sound source one can hear certain artefacts (such as high frequency noise) introduced by the spatialization process. We found that by using a four point interpolation we could obtain results with less distortion.

### 4 Summary and Conclusion

We have seen that by making changes to the cmusic space unit generator, we are able to run Moore's spatial algorithm in real-time. Our major modification was to interpolate the delay times within calculation blocks. We have also modified the ray intersection detection algorithms to better match the original model and have improved its performance. Successful implementations of the algorithm have been ported to the Pd[9] and Max/MSP[13] environments. Our implementation currently runs in a quadraphonic configuration in Pd, under RedHat Linux 7.2 on a 866 MHz Intel Pentium III, utilizing 53% of the CPU (including the overhead of Pd), and in Max/MSP under Mac OS 9.2 on a 400 MHz PowerMac G4 utilizing 37% of the CPU (including the overhead of MAX/MSP).

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\(^1\) Direct is a user definable variable which defines the power laws for calculating distant attenuation values of direct and reflected rays.

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References


